## CS 188: Artificial Intelligence Spring 2010

Lecture 12: Reinforcement Learning II 2/25/2010

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Many slides over the course adapted from either Dan Klein, Stuart Russell or Andrew Moore

#### Announcements

- W3 Utilities: due tonight
- P3 Reinforcement Learning (RL):
  - Out tonight, due Thursday next week
  - You will get to apply RL to:
    - Gridworld agent
    - Crawler
    - Pac-man

## Reinforcement Learning

- Still assume a Markov decision process (MDP):
  - A set of states  $s \in S$
  - A set of actions (per state) A
  - A model T(s,a,s')
  - A reward function R(s,a,s')
- Still looking for a policy  $\pi(s)$
- New twist: don't know T or R
  - . I.e. don't know which states are good or what the actions do
  - Must actually try actions and states out to learn

#### The Story So Far: MDPs and RL

#### Things we know how to do:

- If we know the MDP
  - Compute V\*, Q\*, π\* exactly
  - Evaluate a fixed policy  $\pi$
- If we don't know the MDP
  - We can estimate the MDP then solve
  - We can estimate V for a fixed policy  $\pi$  Model-free RL:
  - We can estimate Q\*(s,a) for the optimal policy while executing an exploration policy

#### Techniques:

- Model-based DPs
  - Value and policy Iteration
  - Policy evaluation

Model-based RL

- Value learning
- Q-learning

## Problems with TD Value Learning

- TD value leaning is a model-free way to do policy evaluation
- · However, if we want to turn values into a (new) policy, we're sunk:



 $\pi(s) = \arg\max_{a} Q^*(s, a)$ 

$$Q^*(s, a) = \sum_{s'} T(s, a, s') \left[ R(s, a, s') + \gamma V^*(s') \right]$$

- Idea: learn Q-values directly
- Makes action selection model-free too!

# **Active Learning**

- Full reinforcement learning
  - You don't know the transitions T(s,a,s')
  - You don't know the rewards R(s,a,s')
  - You can choose any actions you like
  - Goal: learn the optimal policy
  - ... what value iteration did!
- In this case:
  - · Learner makes choices!
  - Fundamental tradeoff: exploration vs. exploitation
  - This is NOT offline planning! You actually take actions in the world and find out what happens...

#### **Detour: Q-Value Iteration**

- Value iteration: find successive approx optimal values
  - Start with  $V_0(s) = 0$ , which we know is right (why?)
  - Given V<sub>i</sub>, calculate the values for all states for depth i+1:

$$V_{i+1}(s) \leftarrow \max_{a} \sum_{s'} T(s, a, s') \left[ R(s, a, s') + \gamma V_i(s') \right]$$

- But Q-values are more useful!

  - Start with Q<sub>0</sub>(s,a) = 0, which we know is right (why?)
     Given Q<sub>i</sub>, calculate the q-values for all q-states for depth i+1:

$$Q_{i+1}(s, a) \leftarrow \sum_{s'} T(s, a, s') \left[ R(s, a, s') + \gamma \max_{a'} Q_i(s', a') \right]$$

### Q-Learning

- Q-Learning: sample-based Q-value iteration
- Learn Q\*(s,a) values
  - Receive a sample (s,a,s',r)
  - Consider your old estimate: Q(s, a)
  - Consider your new sample estimate:

$$\begin{split} Q^*(s,a) &= \sum_{s'} T(s,a,s') \left[ R(s,a,s') + \gamma \max_{a'} Q^*(s',a') \right] \\ sample &= R(s,a,s') + \gamma \max_{a'} Q(s',a') \end{split}$$

• Incorporate the new estimate into a running average:

$$Q(s, a) \leftarrow (1 - \alpha)Q(s, a) + (\alpha) [sample]$$

# Q-Learning Properties

- Amazing result: Q-learning converges to optimal policy
  - If you explore enough
  - If you make the learning rate small enough
  - ... but not decrease it too quickly!
  - Basically doesn't matter how you select actions (!)
- Neat property: off-policy learning
  - learns optimal Q-values, not the values of the policy you are

## Exploration / Exploitation

- Several schemes for forcing exploration
  - Simplest: random actions (ε greedy)
    - Every time step, flip a coin
    - With probability  $\epsilon$ , act randomly
    - With probability 1-ε, act according to current policy
- Regret: expected gap between rewards during learning and rewards from optimal action
  - Q-learning with random actions will converge to optimal values, but possibly very slowly, and will get low rewards on the way
  - Results will be optimal but regret will be large
  - How to make regret small?

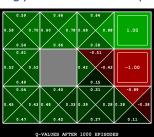
# **Exploration Functions**

- When to explore
  - Random actions: explore a fixed amount
  - · Better ideas: explore areas whose badness is not (yet) established, explore less over time
- One way: exploration function
  - Takes a value estimate and a count, and returns an optimistic utility, e.g. f(u,n) = u + k/n (exact form not important)

$$\begin{split} &Q_{i+1}(s, a) \leftarrow_{\alpha} R(s, a, s') + \gamma \max_{a'} Q_{i}(s', a') \\ &Q_{i+1}(s, a) \leftarrow_{\alpha} R(s, a, s') + \gamma \max_{a'} f(Q_{i}(s', a'), N(s', a')) \end{split}$$

# Q-Learning

• Q-learning produces tables of q-values:



## Recap Q-Learning

- Model-free (temporal difference) learning
  - · Experience world through episodes

$$(s, a, r, s', a', r', s'', a'', r'', s'''' \ldots)$$

- Update estimates each transition (s, a, r, s')
- · Over time, updates will mimic Bellman updates



$$Q_{i+1}(s, a) \leftarrow \sum_{s'} T(s, a, s') \left[ R(s, a, s') + \gamma \max_{a'} Q_i(s', a') \right]$$

Q-Learning (model-free, requires only experienced transitions)

$$Q(s, a) \leftarrow (1 - \alpha)Q(s, a) + (\alpha) \left[ r + \gamma \max_{a'} Q(s', a') \right]$$

## Q-Learning

- In realistic situations, we cannot possibly learn about every single state!
  - Too many states to visit them all in training
  - Too many states to hold the q-tables in memory
- Instead, we want to generalize:
  - Learn about some small number of training states from experience
  - · Generalize that experience to new, similar states
  - This is a fundamental idea in machine learning, and we'll see it over and over again

# Example: Pacman

- Let's say we discover through experience that this state is bad:
- In naïve q learning, we know nothing about this state or its q states:
- Or even this one!







Solution: describe a state using a vector of features (properties)

Feature-Based Representations

- Features are functions from states to real numbers (often 0/1) that capture important properties of the state
- Example features:
- Distance to closest ghost
  Distance to closest dot
- Number of ghosts
   1 / (dist to dot)<sup>2</sup>
- Is Pacman in a tunnel? (0/1)
- . Is it the exact state on this slide?
- Can also describe a q-state (s, a) with features (e.g. action moves closer to food)



### **Linear Feature Functions**

Using a feature representation, we can write a Q function (or value function) for any state using a few weights:

$$V(s) = w_1 f_1(s) + w_2 f_2(s) + \ldots + w_n f_n(s)$$

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \dots + w_n f_n(s,a)$$

- Advantage: our experience is summed up in a few powerful numbers
- Disadvantage: states may share features but actually be very different in value!

**Function Approximation** 

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \dots + w_n f_n(s,a)$$

Q-learning with linear q-functions:

$$\begin{split} & transition = (s, a, r, s') \\ & \text{difference} = \left[r + \gamma \max_{a'} Q(s', a')\right] - Q(s, a) \\ & Q(s, a) \leftarrow Q(s, a) + \alpha \left[\text{difference}\right] \end{split} \quad \text{Exact Q's} \end{split}$$

 $w_i \leftarrow w_i + \alpha$  [difference]  $f_i(s, a)$ 

- Intuitive interpretation:
  - · Adjust weights of active features
  - E.g. if something unexpectedly bad happens, disprefer all states with that state's features
- · Formal justification: online least squares

Approximate Q's

